RATIONALITY OF PROPER HOLOMORPHIC MAPS BETWEEN BOUNDED SYMMETRIC DOMAINS

Sung-Yeon Kim

(Institute for Basic Science, Korea)

Abstract: In this talk, we study the rationality of a proper holomorphic map $f: \Omega \to \Omega'$ between irreducible bounded symmetric domains Ω and Ω' that maps Shilov boundary to Shilov boundary. More precisely, we show that if Ω and Ω' are of type one with rank greater or equal to two and $f: \Omega \to \Omega'$ extends smoothly to the boundary sending Shilov boundary to Shilov boundary, then f is of the form $f = i \cdot F$, where $F = F_1 \times F_2 : \Omega \to \Omega'_1 \times \Omega'_2$, Ω'_1, Ω'_2 are bounded symmetric domains, $F_1: \Omega \to \Omega'_1$ is a rational proper embedding with respect to canonical K ahler-Einstein metrics. Moreover if Ω is not of tube type, then f is a rational map.